



Representational Biases under Proportional Representation

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Parliamentary Representation and Electoral Systems

- PR delivers well on indicators of representation
 - Congruence
 - Disproportionality
 - Party system fractionalization (ENP)
- Common version of PR: districted PR
 - employed by more than half of democratic states



Parliamentary Representation under Districted PR (I)

- The study of representation treats districted PR as national-district PR
 - When evaluating representation across countries, votes are identified by the party for which they are cast
- However:
 - (1) Interests are districted: voters', MP's, and parties'
 - (2) Institutions vary by district: heterogeneity in district magnitude (DM) within states
- These two facts have implications for the study of representation



Parliamentary Representation under Districted PR (II)

(1) Interests are district-specific

(2) Institutions converting votes to seats vary by district

- Large heterogeneity within countries: same representation on average, but fraction of parliament elected by small / large districts differ across countries
- Incorporate these into the study of representation:
 - Party system fragmentation
 - Disproportionality
 - Inequality in representation (today)



Today: Are Voters Equal under Proportional Representation?

in collaboration with Liran Harsgor, Raz Sheinerman

Two basic Questions

Are voters under proportional representation equally represented in parliament?

- (i) Is there a systematic ideological bias in representation under PR?
- (ii) What districting principles enhance representational equality among voters?



A New Approach to Evaluating Parliamentary Representation: Main Findings

Key findings

1. Under districted PR, compared to the electorate the parliamentary pie is often biased in favor of supporters of right-leaning parties (and large parties)
2. Irrespective of the median (or avg.) district, the fraction of parliament elected via small districts affects representational inequality.



Geographically Motivated Representation under PR

- **Voters**
 - Vary in their interest by region (more on this below)
- **Parties** often have to prioritize interests that correlate with districts
 - Subsidize industry vs. agriculture
 - Invest in north or south
 - Pork
- **MP's** are not district-blind in their efforts
 - Bowler and Farrell (1993)
 - Strattman and Baur (2002)
 - Heitshusen et al. (2005)
 - Shugart et al. (2005) on personal vote



Evaluating Representation under Districted Systems: Setup

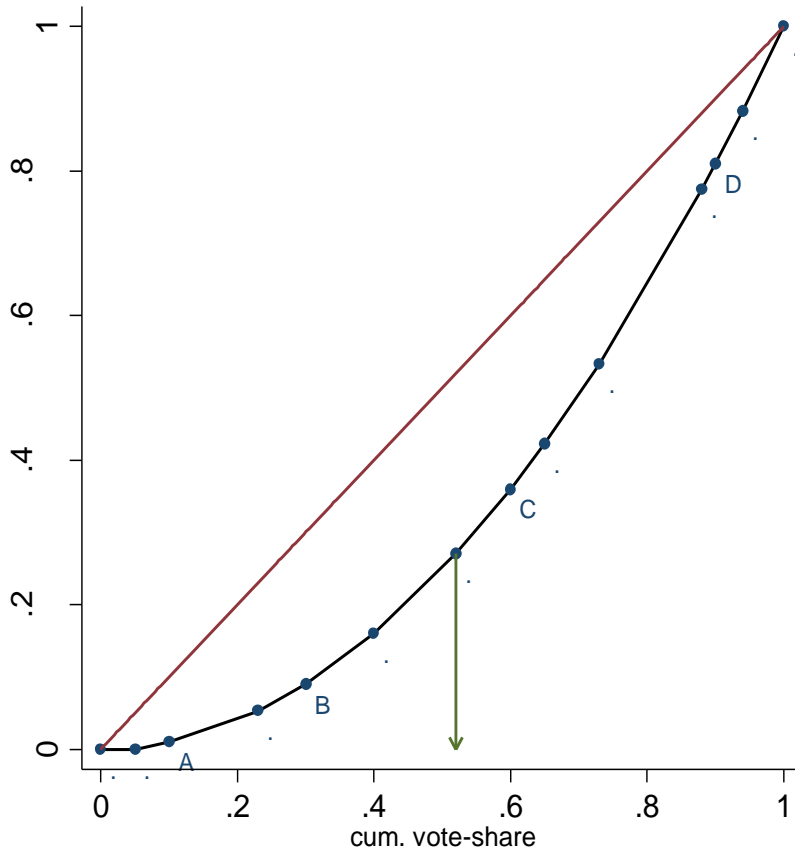
	p_1	p_2	.. p_K	Total
d_1	V_{11}, S_{11}	V_{12}, S_{12}		
d_2	V_{21}, S_{21}	V_{22}, S_{22}		
\vdots				
d_N				
Total				V, S

Conversion Ratio (CR): seat-share/vote-share

e.g., $\frac{s_{11}/S}{v_{11}/V}$



Representational Inequality (RI)



- inequality curve
 - conversion ratio (CR): seat-share/vote-share
 - How many are underrepresented?
 - By how much are they underrepresented?
- RI summary index (area)
- voters supporting different parties residing in same district (A, B)
 - are seats occupied by those parties that voters supported?
- voters supporting the same party residing in different districts (A,C)
 - does the party in parliament reflect its electoral base of support?
- any two voters (A,D)



Representational Inequality: Hypotheses

Within countries

(i) Whose voice is louder?

H1: In countries characterized by substantial variation in DM, supporters of right-wing parties are overrepresented compared with their left-wing counterparts, and the effect declines with district magnitude

- Monroe and Rose (2002)
- Rodden (2010)

Across countries

(ii) How does the districting structure affect representational inequality?

H2: The greater the share of parliament elected via small districts the greater is inequality



Focus on Districted PR

Advantages

- Prevalence
 - 70% of democracies have proportional representation (PR)
 - 80% of PR systems are districted
- Variation in distribution of DM across countries
- The literature often categorizes electoral systems by middle district

Challenges

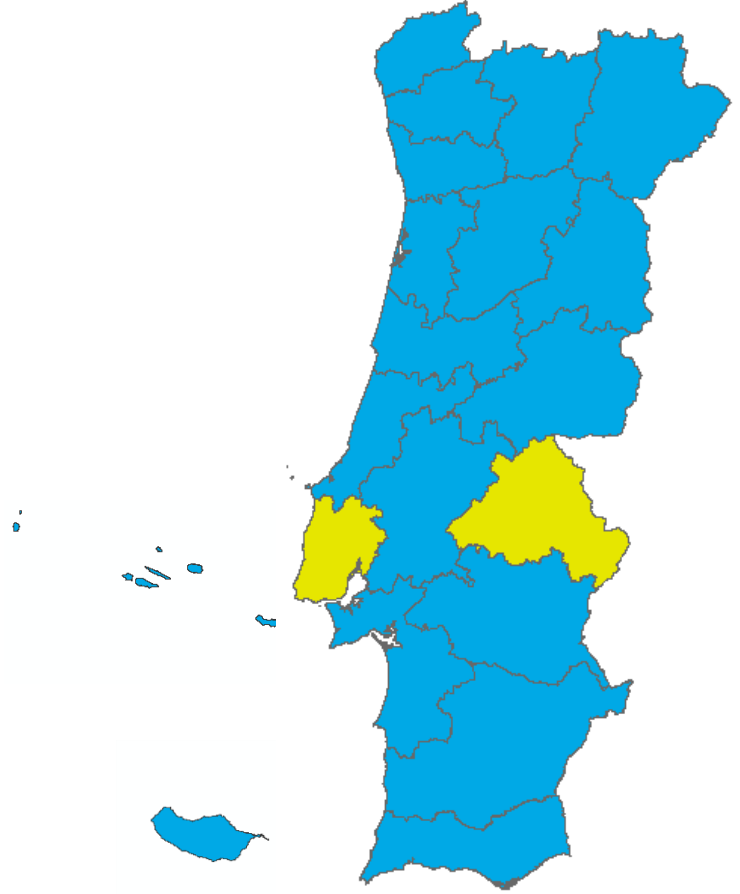
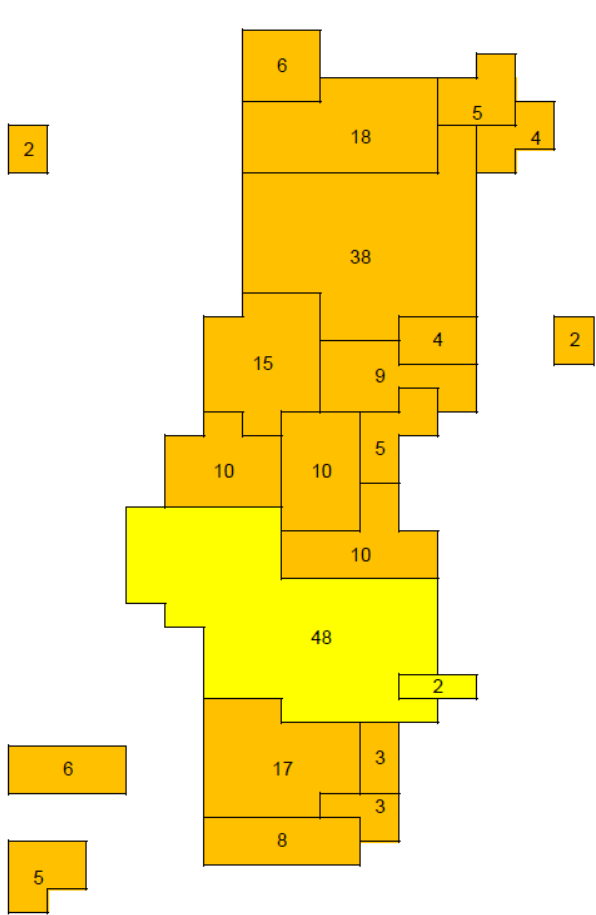
- Compensatory seats (as separate districts or added to current districts)
- Variation in other mechanisms (formula, malapportionment, threshold...)



Example: Portugal (22 Electoral Districts)



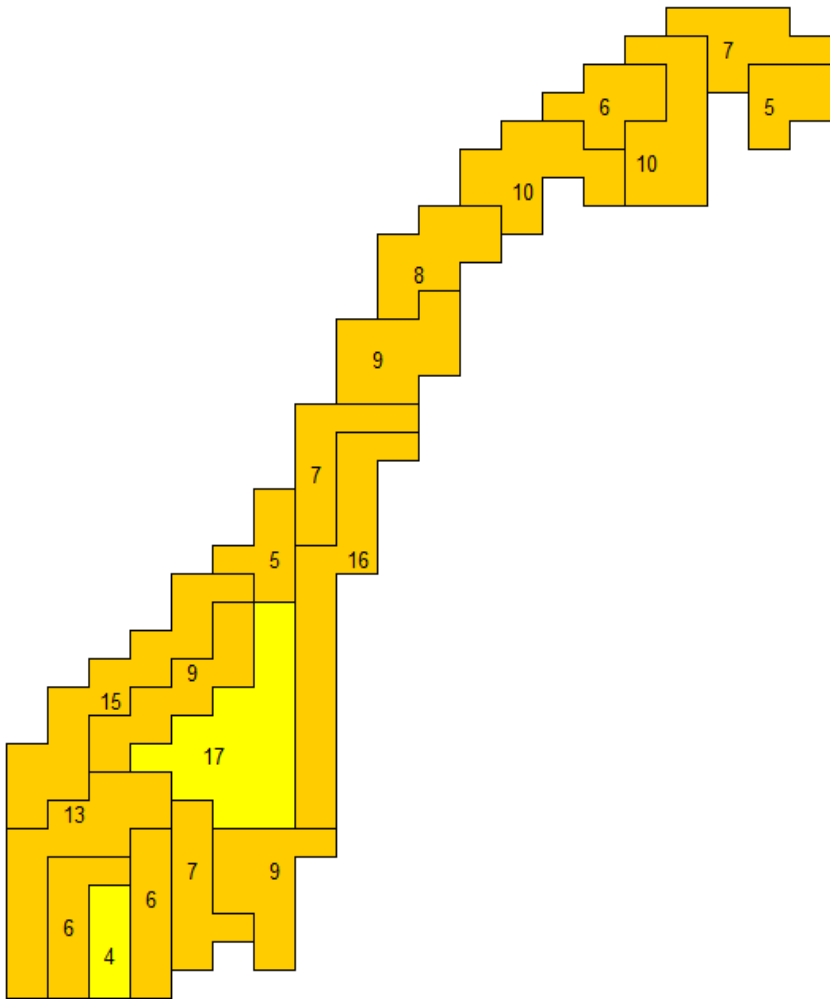
Example: Portugal (22 Electoral Districts)



Norway: 19 Electoral Districts

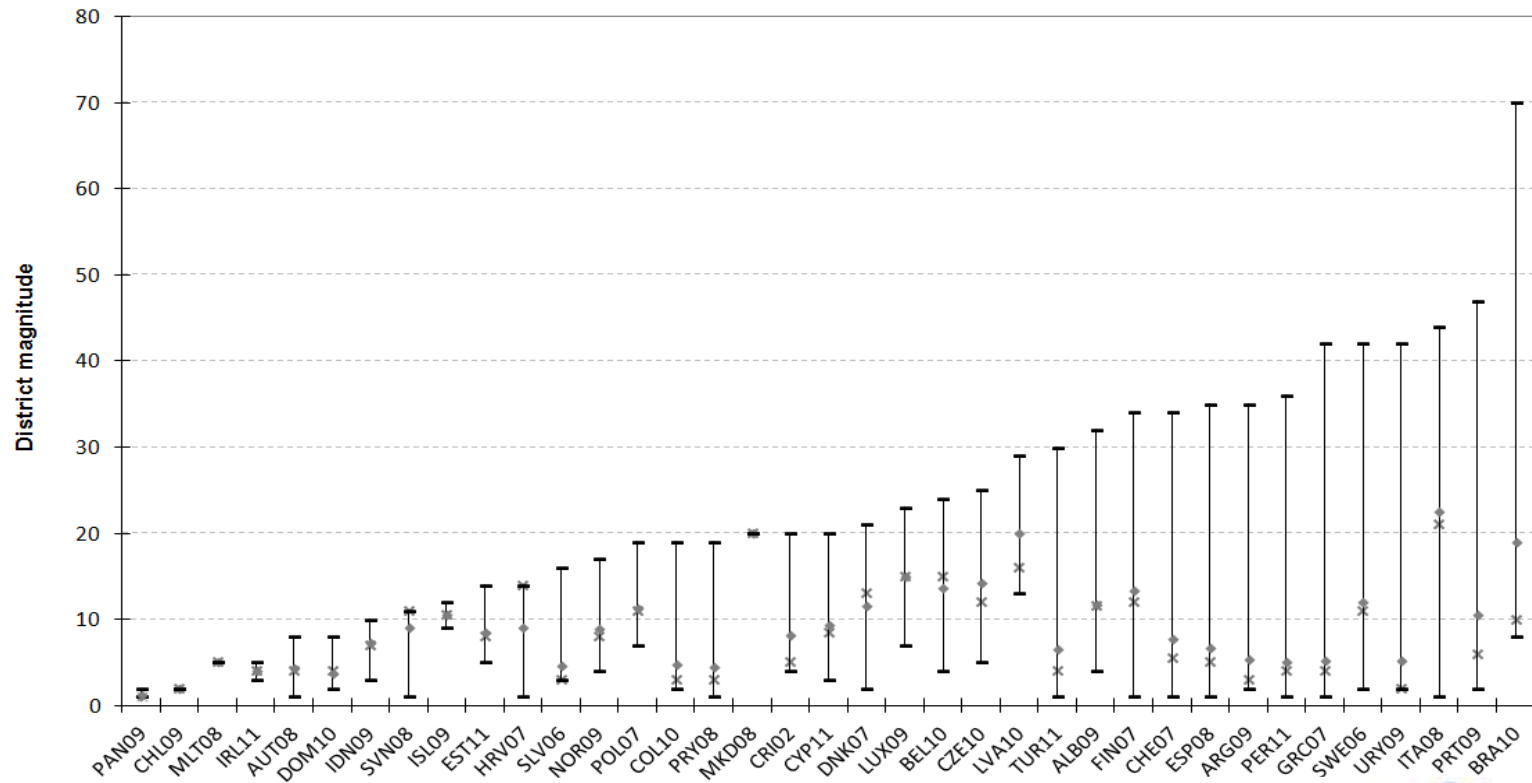


Norway: 19 Electoral Districts

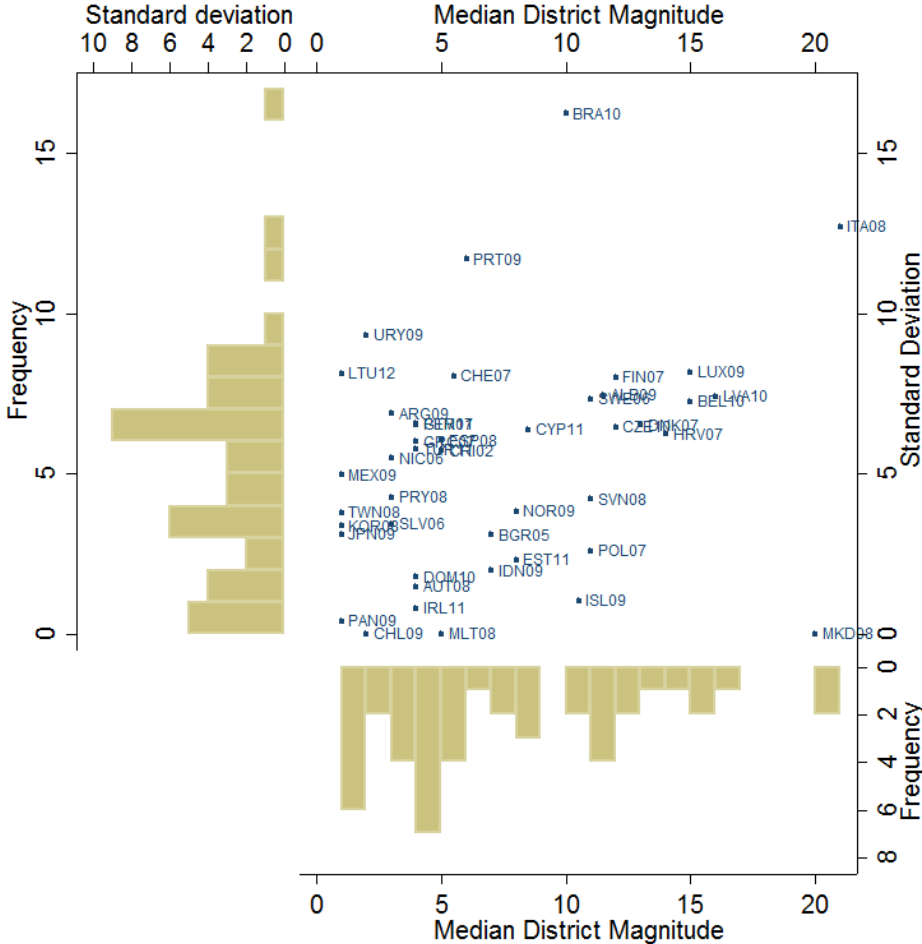


District magnitude in Districted PR's

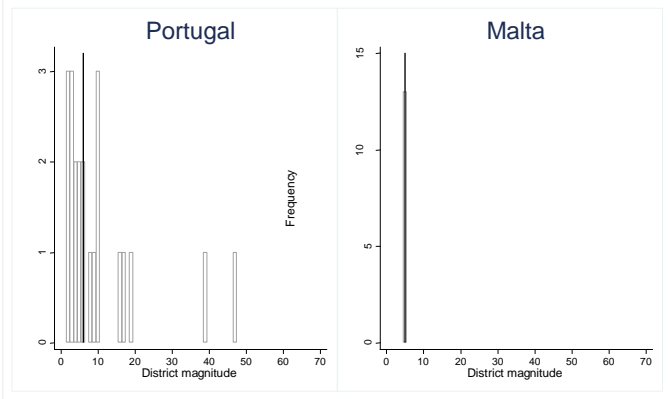
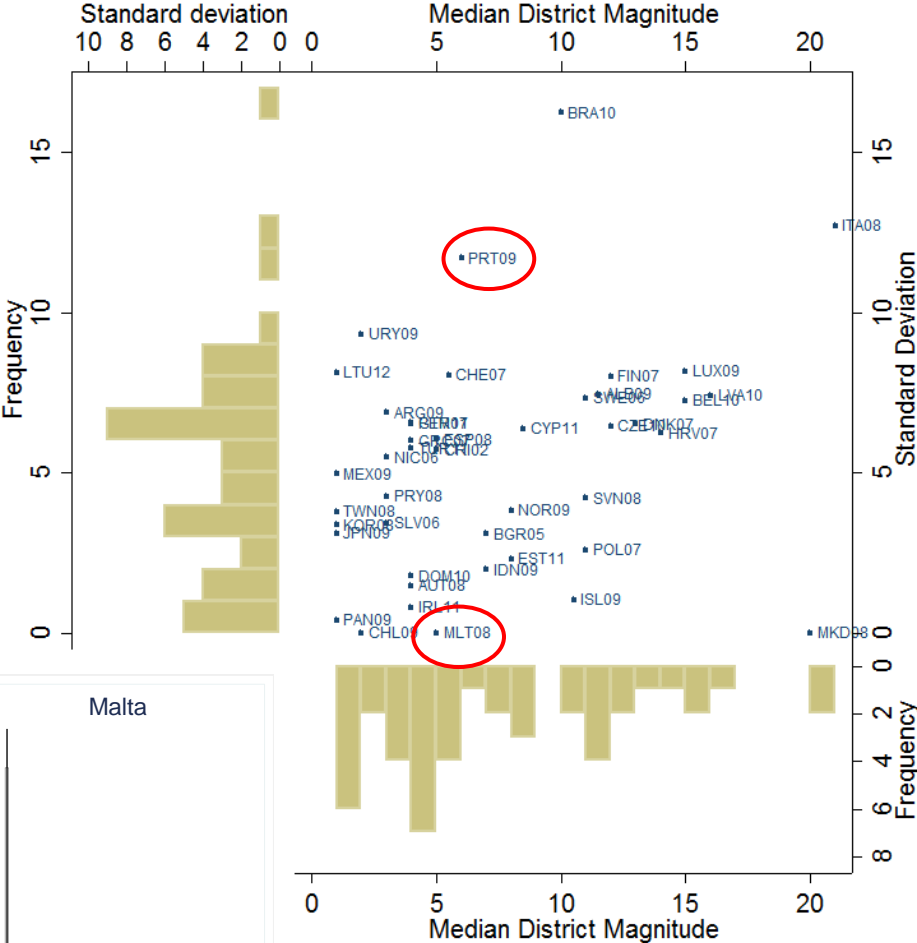
District magnitude: minimum, median (x), average (◆), maximum



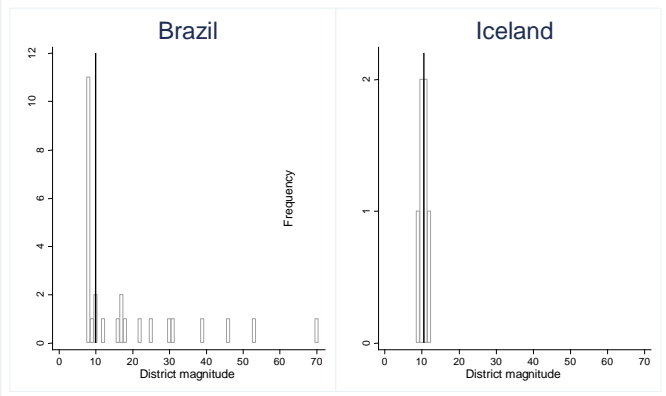
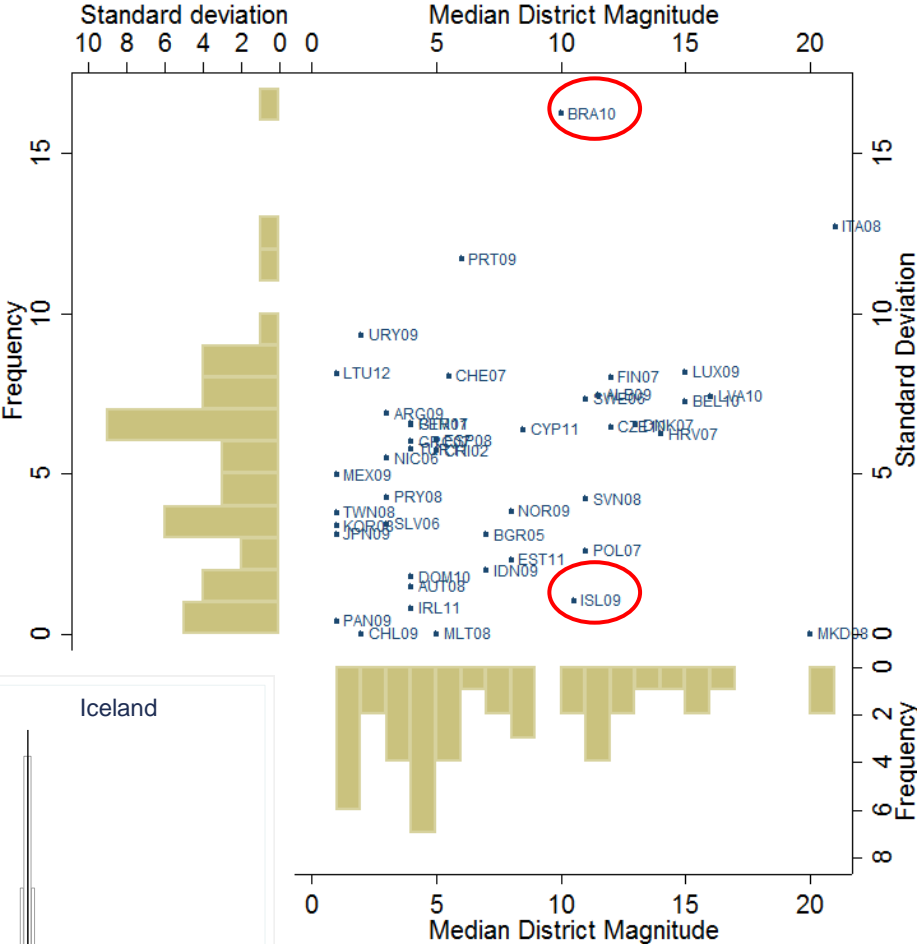
District magnitudes: medians and standard deviations (Districted PR + mixed systems)



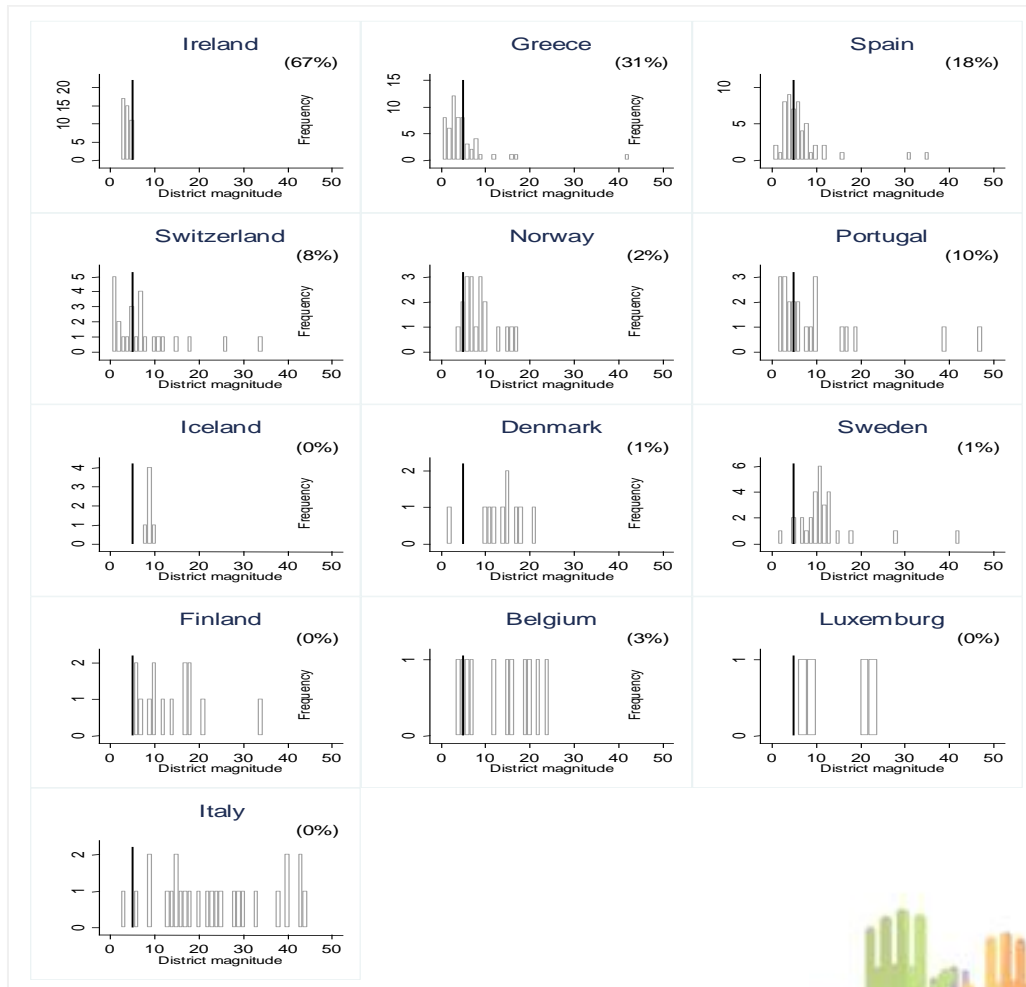
District magnitudes: medians and standard deviations (Districted PR + mixed systems)



District magnitudes: medians and standard deviations (Districted PR + mixed systems)



Distributions of District Magnitude under Districted PR (Western Europe)



Data used (here)

- Election results (votes, seats) at the district level per country
 - 236 parties (158 in parliaments)
 - 1391 districts (330 in districted PR)
 - 20 Countries:
 - Districted PR:** Belgium (2010), Denmark (2007), Finland (2007), Greece (2007), Iceland (2009), Ireland (2011), Italy (2008), Luxemburg (2009), Malta (2008), Norway (2009), Spain (2008), Sweden (2006), Switzerland (2007), Portugal (2009)
 - Complemented by**
 - National-district PR:** Germany (2009), Israel (2009), New Zealand (1996), the Netherlands (2010)
 - Majoritarian:** Canada (2011), New Zealand (1993), the UK (2010)



i. Whose Voice Is Louder?

H1: In countries with large variation in DM, supporters of right-wing parties are overrepresented and especially so in small districts

- ideological L-R placement coding of parties based on manifestos (Benoit and Laver, 2006). Also, expert survey of ideological party placement (Chapel Hill dataset)
- estimate:

$$CR_{ij} = b_0 + b_1 \ln(dm_i) + b_2 partyLR_j + b_3 \ln(dm_i) * partyLR_j$$

- QoI: the association between ideology and conversion ratio

$$\frac{\partial CR_{ij}}{\partial partyLR_j} = b_2 + b_3 \ln(dm_i)$$

- should see

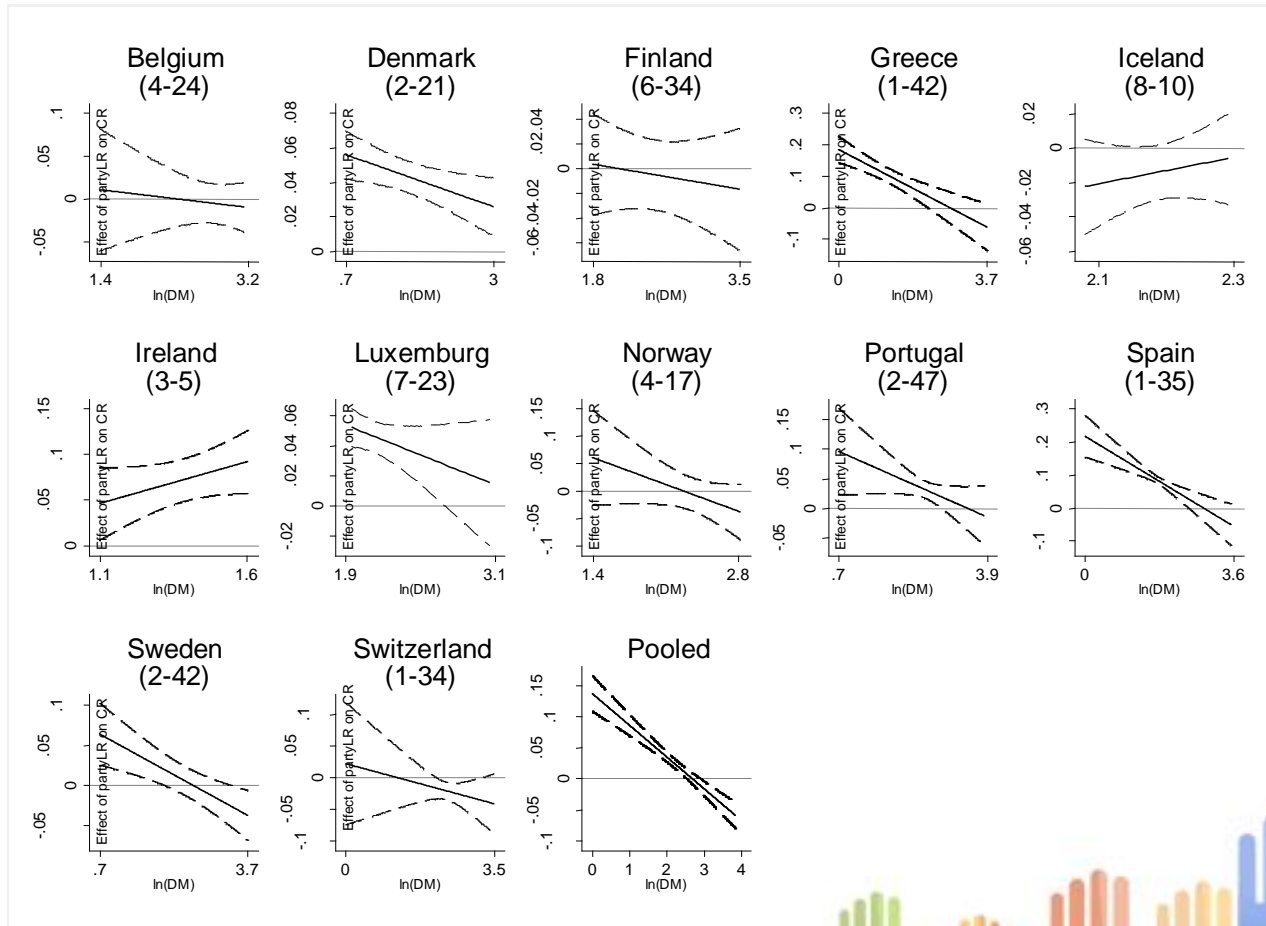
small districts: $CR(R) > 1$, $CR(L) < 1$

large districts: no relationship



i. Whose Voice Is Louder?

The Effect of Party Ideology on Vote-to-Seat Conversion



ii. Cross Country: How Does Districting Structure Affect Representational Inequality?

H2: The greater the share of parliament elected via small districts the greater is inequality

$$RI_c = b_0 + b_1 \text{ "hump" }_c + b_2 \ln(dm_c) + CTRLs$$

Model	% legislators elected in districts <7, 5, 3		Central DM (med. Leg.)	STV	Electoral formula (Lijphart)	Constant	R ²
i			-0.08 (0.02)	-0.10 (0.07)	0.02 (0.07)	0.41 (0.09)	0.77
ii	%<7	0.32 (0.09)	-0.04 (0.02)	-0.31 (0.08)	-0.02 (0.02)	0.31 (0.07)	0.88
iii	%<5	0.36 (0.03)	-0.04 (0.01)	-0.11 (0.03)	-0.03 (0.01)	0.34 (0.03)	0.97
iv	%<3	0.31 (0.06)	-0.05 (0.01)	-0.02 (0.05)	-0.02 (0.02)	0.37 (0.06)	0.91

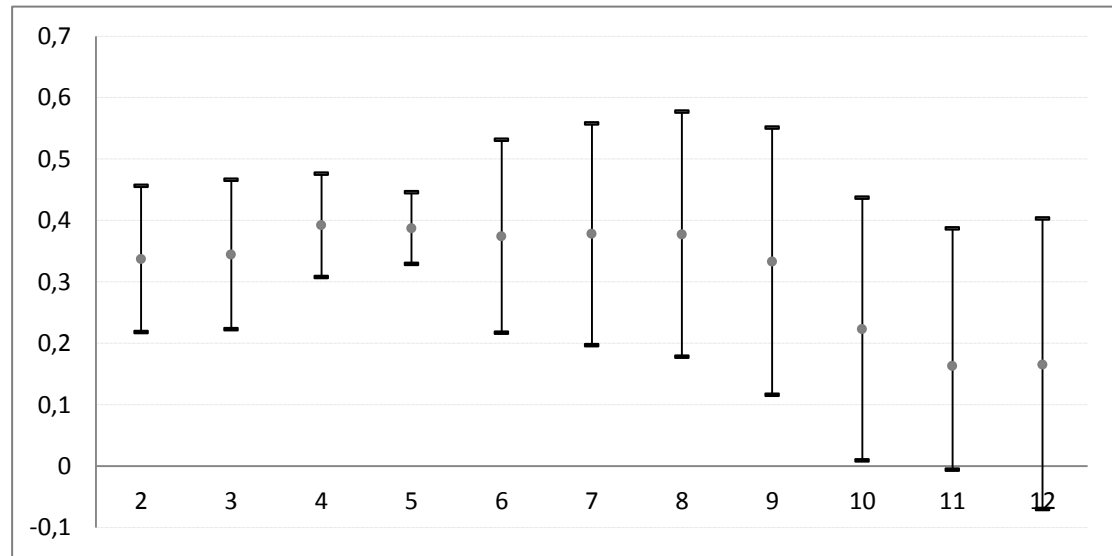
* N=21. Robustness: avg. DM, med. DM, alternative electoral formula coding (Rae, Gallagher, Benoit).



Representational Inequality and Small Districts:

Alternative Cutoff Points

b_1 : the effect of fraction of parliament elected in small districts on RI



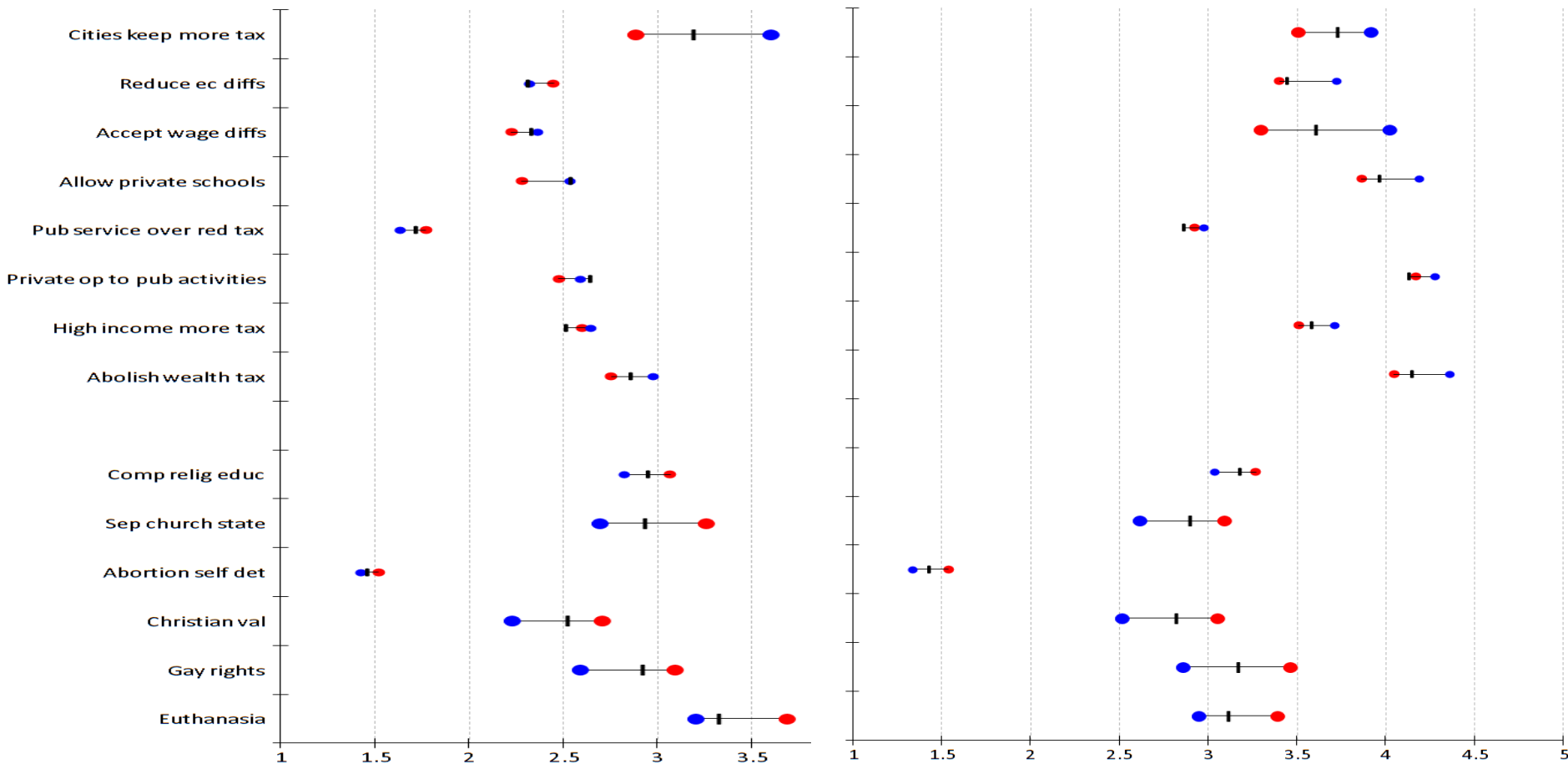
Cutoff district magnitude



Norway 2009: Policy Positions among Co-partisans Residing in Different Regions

Labour supporters

Conservatives supporters



Oslo vs. West. 1= ec. left, soc. liberal



Conclusion: Unequal Representation of Voters

- The parliamentary pie is often biased in favor of right-leaning (and large) parties compared with the distribution of votes.
 - Bias originates mostly in small districts
- Across countries: the greater the share of parliament elected via small districts the greater is inequality, irrespective of magnitude of central district.
- Voters across regions (districts) differ in their positions so over/under representation does not cancel out.
- Representation is not an 'on average' quantity.

